

Does Counting Still Count?

Revisiting the Security of Counting based User Authentication Protocols against Statistical Attacks

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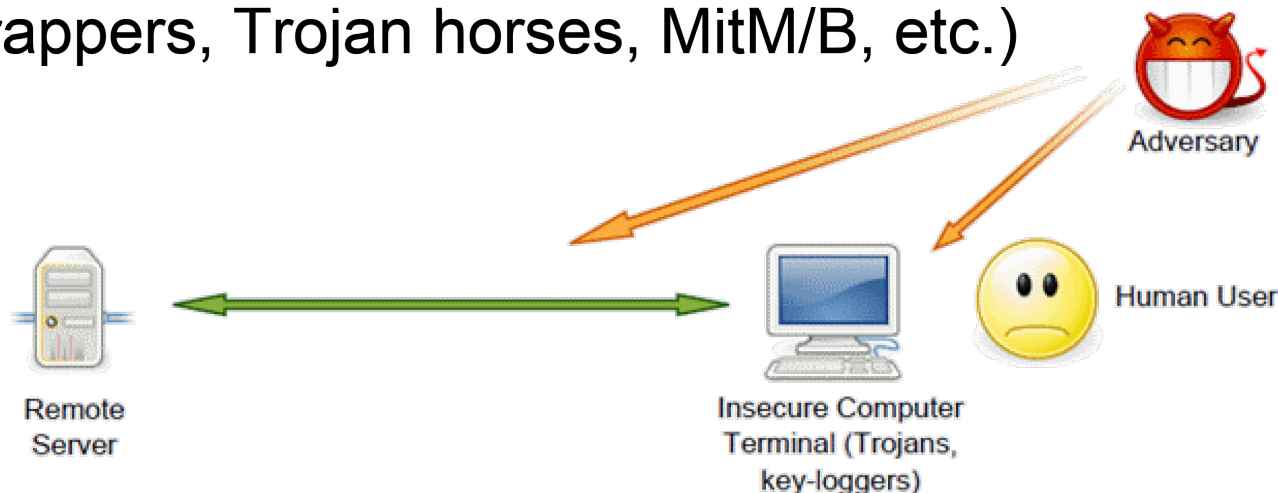
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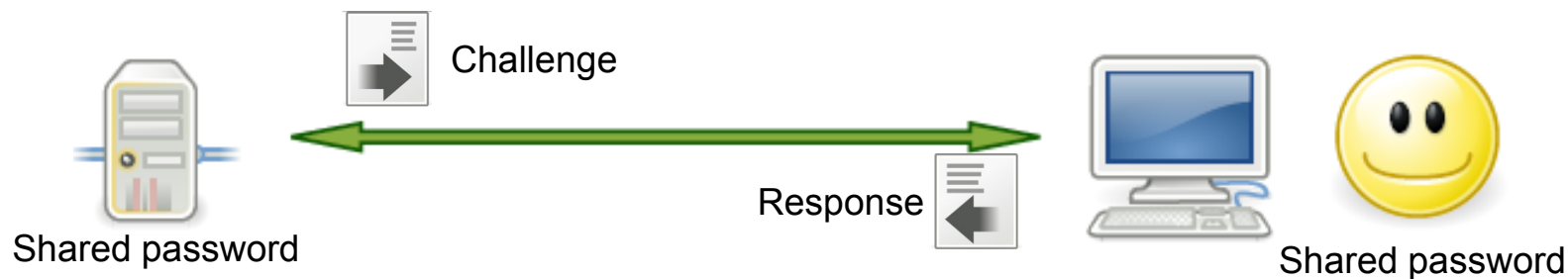
- An Old Problem: Unassisted Human Authentication against Observers (1990s-)
- A New Threat: Yan et al.'s 2D Statistical Attack (NDSS 2012)
- Our Contributions
 - Why does Yan et al.'s attack work? – A general theoretical analysis of δ D statistical attacks ($\delta \geq 1$) on counting based protocols
 - An approach for estimating the security bound
 - New principles and fixes to make counting based protocols more secure against the new attacks

The (old) problem

- How to authenticate an **unassisted** human user on an **observable** (untrusted) terminal?
 - Why **unassisted**? – Hardware devices cause usability problems and may be attacked as well.
 - Who are **observers**? – Shoulder surfers, hidden cameras, card skimmers, malware (keyloggers, screen scrappers, Trojan horses, MitM/B, etc.)



- Challenge-response protocols proposed as general solutions to hide the shared secret P in challenges $C=f_C(P)$ and responses $R=f_R(P,C)$.



- Many solutions exist, but the main research question remains **unanswered**:
 - How to make a protocol which is both usable and secure against adversary with **many** observed sessions?

Solutions based on counting?

- Many proposed solutions follow this approach.
- Password $P = k$ pass-objects out of n objects
- Challenge $C = l$ objects ($l \leq n$)
- Response R
 - Count pass-objects P in $C \Rightarrow \#C(P)$
 - Response $R = f_R(\#C(P))$, e.g. $R = \#C(P) \bmod 2$
- Why counting?
 - Recognizing objects and counting are believed easy tasks for most human users!

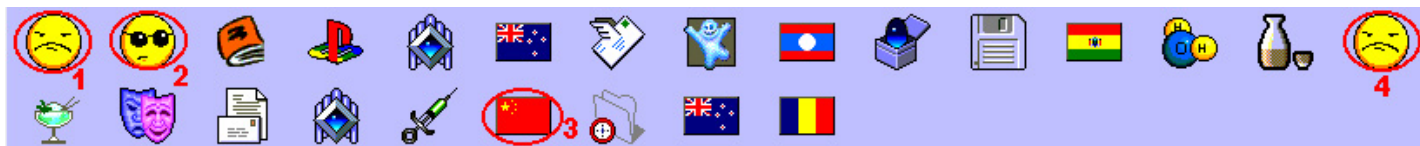




A typical counting based protocol

- Proposed by Li & Shum in 2001/2002 (published as IACR ePrint 2005/268)
- Claimed to be secure: given $O(n)$ observed sessions, the adversary's chance of success is 2^{-n} .
- Usability is better than other solutions with similar security, but still not practical (2-3 minutes).
- At NDSS 2012 Yan et al. reported a statistical attack which can fully recover P with $O(n)$ observed sessions.
 - The attack can be generalized to other counting based protocols.

- Challenge C of size $2l = C_1 + C_2$ (each of size l)
 - Uni-Rule: C_1 is generated such that there are 0, 1, 2 or 3 pass-objects with equal probability.
 - Rand-Rule: C_2 is generated at random (the number of pass-objects can be anything from 0 to $\min(k, l)$).
- Response R
 - $R=0$ if $\#C(P) \bmod 4 = 0$ or 1 , otherwise $R=1$
- Example



- For the above challenge C , the response $R=0$.

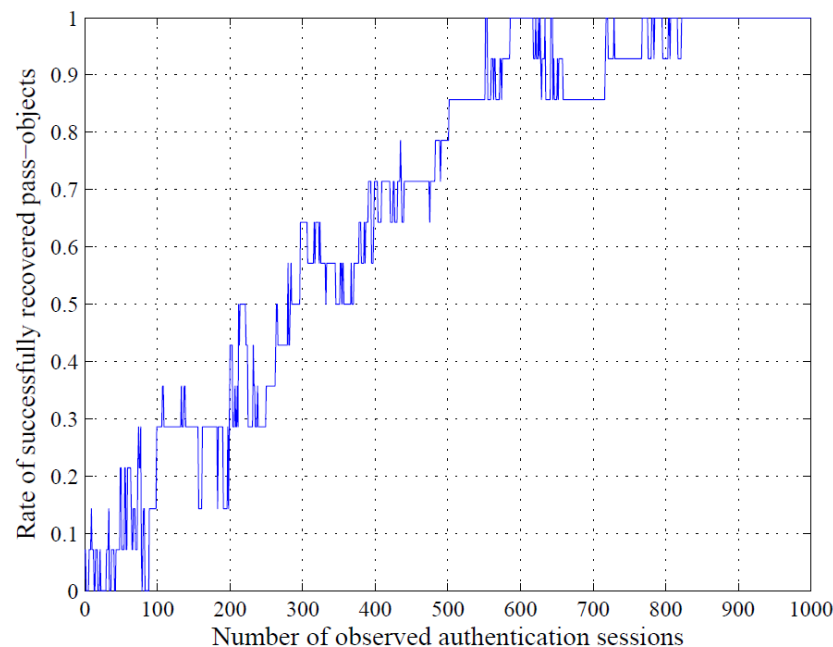
How does Yan et al.'s attack work?

- Based on counting as well (but in 2D space)!
 - For Response 0 and 1, count the occurrences of each **object pair** (o_1, o_2) in each challenge to get F_1 and F_2 .
 - Rank all objects pairs according to $F_1 - F_2$.
 - Take the top k distinct objects as the password.
- Why does it work?
 - No theoretical explanation, but Yan et al.'s experiments revealed pass-object pairs tend to produce larger $F_1 - F_2$.

| Object Pairs | 0-response | 1-response | Difference |
|--------------|------------|------------|------------|
| (1, 2) | 28 | 24 | +4 |
| (1, 3) | 32 | 26 | +6 |
| : | : | : | : |
| ($n-1, n$) | 40 | 28 | +12 |

How well does Yan et al.'s attack work to break Foxtail?

- Parameters of Foxtail: $(n,k,l)=(140,14,15)$
- Results
 - Password recovered in about 711 authentication sessions using 2D frequency tables
 - 90% of pass-objects recovered in about 540 sessions



Our contributions

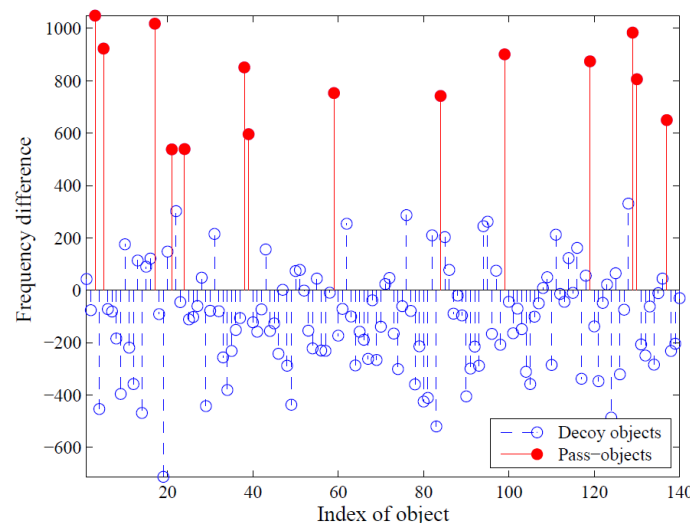
- Why does Yan et al.'s attack work?
 - Yan et al.'s 2D attack \Rightarrow δ D attacks ($\delta \geq 1$)
 - 1D attack works as well! \Rightarrow Yan et al.'s 2D attack is just a generalization of the 1D attack to 2D space!
 - A general theoretical analysis of δ D attacks
- A theoretical approach for estimating the security lower bound against δ D attacks
 - This presentation will not cover this part due to time limit.
- Two new principles of designing new protocols
- Fixes to make counting based protocols more secure against δ D attacks (so to make counting still work)

Why does Yan et al.'s attack work?

- Three equalities about each object's occurrence frequency must hold to disable each δ D attack
 - $\xi_{\text{pass}}(0) = \xi_{\text{decoy}}(0)$
 - $\xi_{\text{pass}}(1) = \xi_{\text{decoy}}(1)$
 - $\xi_{\text{pass}}(0) - \xi_{\text{pass}}(1) = \xi_{\text{decoy}}(0) - \xi_{\text{decoy}}(1)$
- $3\delta_{\text{max}}$ equalities, but only 3 parameters (n, k, l)
- Yan et al.'s attack works because **none** of the above equalities holds when $\delta=2$!
- \Rightarrow Both theoretical and experimental analysis revealed that Foxtail can **never** be made absolutely secure against δ D attacks!

1D attack works as well!

- 1D attack also works!
 - For the default parameter $(n,k,l)=(140,14,15)$, the password was recovered after about 7,000 authentication sessions were observed.
 - Less efficient than 2D attack, but still a theoretical threat!
- Further analysis shows when $\delta > 2$, the attack still works but the number of required sessions increases drastically.



Beyond response dependent attacks and Foxtail

- The δD attacks discussed so far treat challenges corresponding to different response values separately.
- We can also treat all challenges equally without considering the response values.
- \Rightarrow Two classes of statistical attacks
 - δD RDFA = Response **dependent** frequency analysis
 - δD RIFA = Response **independent** frequency analysis
- Foxtail was designed with only 1D RIFA in mind.
- Both attacks can be applied to many other protocols (not only counting based).

Two new principles for designing protocols based on counting

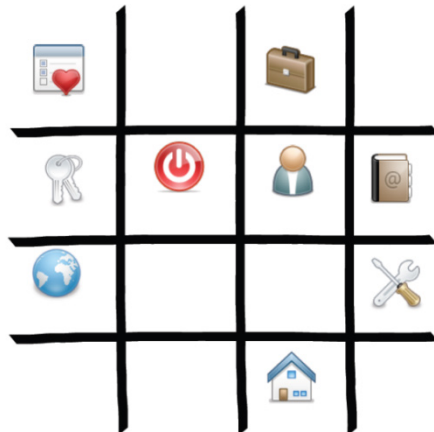
1. Each **object** should be sampled **independently** with the same probability regardless of its type (pass- or decoy objects).
 - This is to prevent RIFA.
2. The **response** should be **independent** of the number of pass-objects in each challenge.
 - This is to prevent RDFA.
 - It seems contradictory, but we will see how it may not be so.

A general fix to any counting based protocols with binary responses

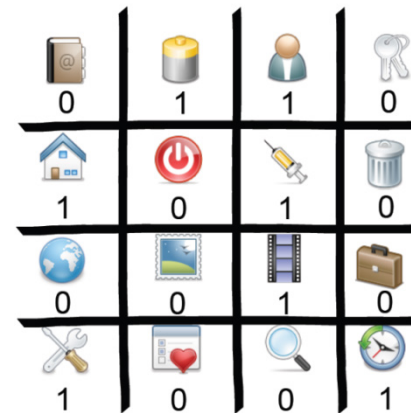
- Generate challenges without distinguishing between pass- and decoy objects
 - Rand-Rule: select l objects at random
 - Each object appears with the same probability p (l will be session varying if $p < 1$)
- Flip the response by a hidden bit (challenge)
 - The (binary) response is flipped according to a random hidden bit (which can be seen as a hidden challenge).
 - This makes responses independent of the number of pass-objects present in the challenge.
- If the response is not binary, the random hidden bit will be replaced by a random hidden variable.

How to generate the random hidden bit?

- Ideally, an out-of-band (OOB) channel can be used.
 - This idea was proposed by some other researchers at CHI 2008 to design a solution based on hidden challenges.
- If an OOB channel is not acceptable or impossible, the flip bit has to be hidden in the public challenge.
 - Below is an example for Foxtail.



First challenge



Second (or flip-bit) challenge

A fix to the fix

- The implementation of the fix without an OOB channel is actually still insecure.
 - The adversary can guess the position of the flip bit.
 - If the guess is wrong, nothing happens.
 - If the guess is correct, it will contribute to the frequency difference between pass- and decoy objects.
 - Experimentally validated, so it is a real threat.
- A possible fix to the fix
 - Use $m > 1$ flip bits instead of just one.
 - When $m = k$, the adversary will have to guess the whole password so have no advantage by guessing the m bits.
 - Usability suffers: authentication time increases.

Yet another (less generic) fix to Foxtail protocol (1)

- Foxtail 2.1: The fixed Foxtail protocol
 - All objects appear in each challenge.
 - Each object is assigned a random weight in $\{0,1,2,3\}$.
 - The response function is changed to the sum of the weights of all pass-objects mod 4.
- Is this enhanced Foxtail secure?
 - Secure against δD RIFA for any $1 \leq \delta \leq k$.
 - Secure against δD RDFA when $\delta < k$.
 - “Insecure” against kD RDFA, but in this case the attacking complexity is the same as brute forcing the password. \Rightarrow Secure against kD RDFA as well.
- Usability suffers: challenges are large.

Yet another (less generic) fix to Foxtail protocol (2)

- Foxtail 2.2: The fixed Foxtail protocol
 - Only l objects appear in each challenge.
 - Each object is assigned a random weight in $\{0,1,2,3\}$.
 - Rand-Rule is used to select the l objects.
 - The response function is changed to the sum of the weights of all pass-objects mod 4.
- Is this enhanced Foxtail secure?
 - Secure against δ D RIFA for any $1 \leq \delta \leq k$.
 - Theoretically insecure against δ D RDFA for any $1 \leq \delta \leq k$.
 - >2,000 sessions are needed to launch a successful attack when $(n,k,l)=(140,14,20)$. \Rightarrow **Practically** secure!
- Usability improves: challenges are smaller.

Usability and future work

- At NDSS 2012 Yan et al. also proposed a framework for estimating usability of human authentication protocols without running any real user study.
- The estimated authentication times
 - Original insecure Foxtail: 213 seconds
 - Foxtail 2.1: 475 seconds
 - Foxtail 2.2: 274 seconds
- Foxtail 2.2 is practical secure and slightly less usable than the original Foxtail.
- Open questions for future work: 1) are there other attacks to Foxtail 2.x? 2) how can we do better?

Thanks for your attention!

